

PERSISTENCY AS A REFERENCE IN DETERMINING RARE EVENT FORECASTING SKILL

Iris Odak Plenković¹, Zoran Pasarić²

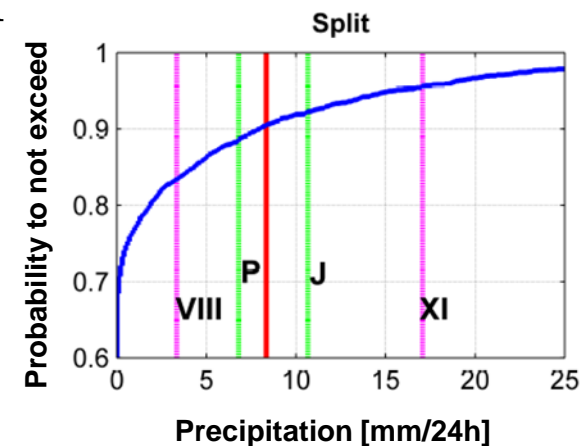
¹ Meteorological and Hydrological Service (DHMZ) of Croatia, Zagreb, Croatia

² AMGI, Department of Geophysics, Faculty of Science, University of Zagreb, Zagreb, Croatia

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INTRODUCTION

- Verification: skill score
- Referent forecast:
 - Random chance, climatological mean, persistence
- Verification of the precipitation forecast (24h accumulation):
 - ALADIN regional model (2008.-2011.)
8 km horizontal resolution, 37 vertical levels,
 - ECMWF global model (2007.-2011.)
0.25° horizontal resolution, 62 vertical levels
 - Locations: Rijeka, Split, Zagreb, Osijek
- Categories:
 - Dry (< 0.2 mm / 24 h)
 - Light precipitation
 - Heavy precipitation



METHODS

- Contingency tables

- Verification measures:

- Climatological probability:

$$P_{\text{dry}} = M/P$$

- Accuracy (Percent Correct):

$$ACC = 100\% * (A+F+K)/P$$

- Frequency Bias:

$$F_{\text{bias}_{\text{dry}}} = D/M$$

- Critical Success Indeks (Threat Score):

$$CSI_{\text{dry}} = A/(D+M-A)$$

- Polychoric Correlation Coefficient:

PCC – measure of association

		OBSERVATIONS			
		DRY	LIGHT	HEAVY	Σ
FORECAST	DRY	A	B	C	D
	LIGHT	E	F	G	H
	HEAVY	I	J	K	L
	Σ	M	N	O	P

perfect forecast:
(100%)

(1)

(1)

(1)



METHODS

- Skill Score – random chance as referent forecast:

- Heidke Skill Score:
$$\mathbf{HSS} = \frac{A+F+K-(MD+NH+OL)/P}{P-(MD+NH+OL)/P} \quad (1)$$

- Pierce Skill Score
(True Skill Score, True Skill

Statistic, Kuipers Skill Score):
$$\mathbf{PSS} = \frac{A+F+K-(MD+NH+OL)/P}{P-(M^2+N^2+O^2)/P} \quad (1)$$

- Stable Equitable Error in Probability Space: **(1-SEEPS)** (1)

- Skill score – persistence as referent forecast:

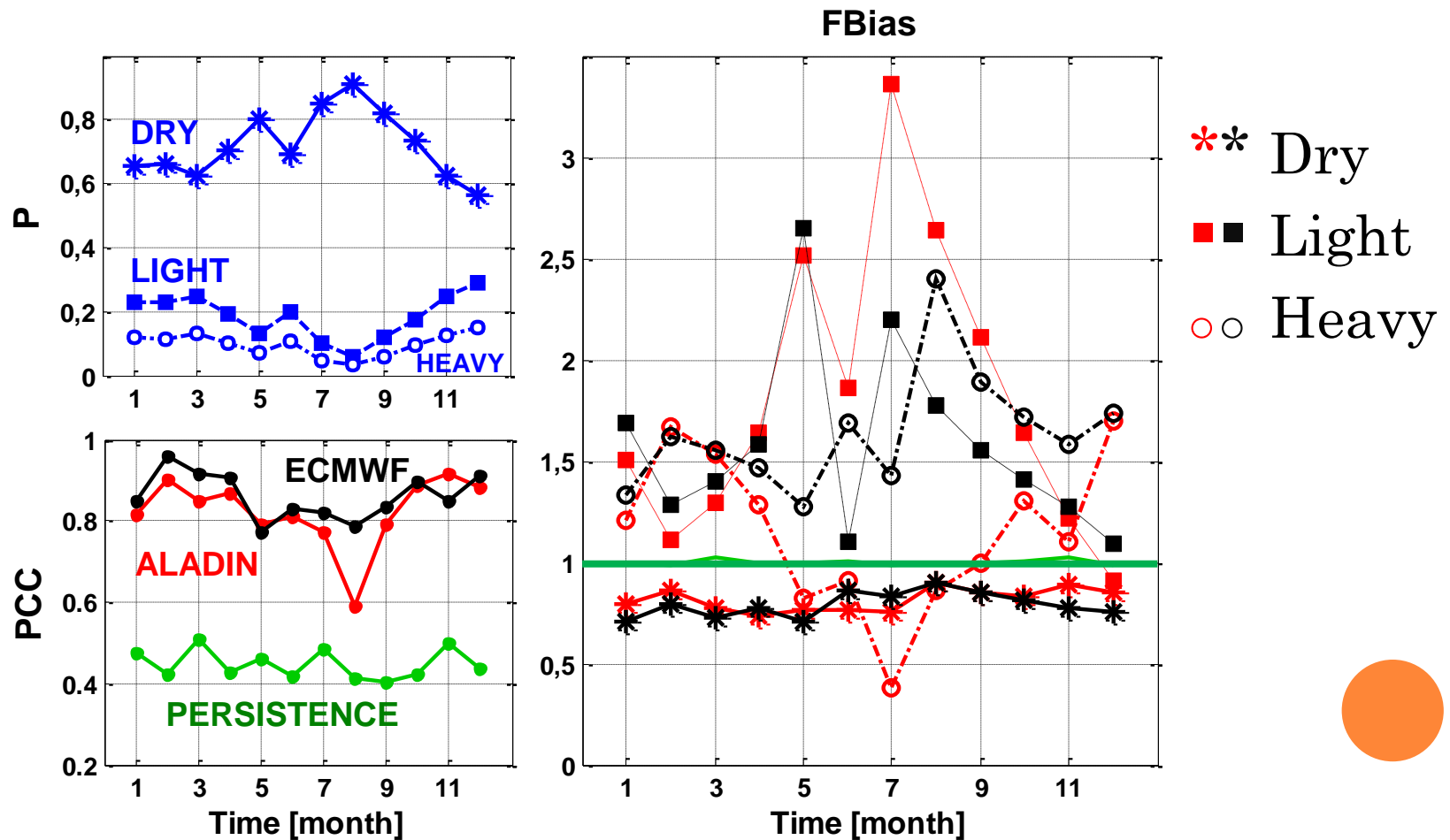
$$\mathbf{pSS} = \frac{SS_{model} - SS_{pers.}}{SS_{ideal} - SS_{pers.}}$$

- pCSI,
- pPCC,
- pHSS,
- pPSS,
- pSEEPS

		OBSERVATIONS			
		DRY	LIGHT	HEAVY	Σ
FORECAST	DRY	A	B	C	D
	LIGHT	E	F	G	H
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	Σ	M	N	O	P

VERIFICATION: SPLIT

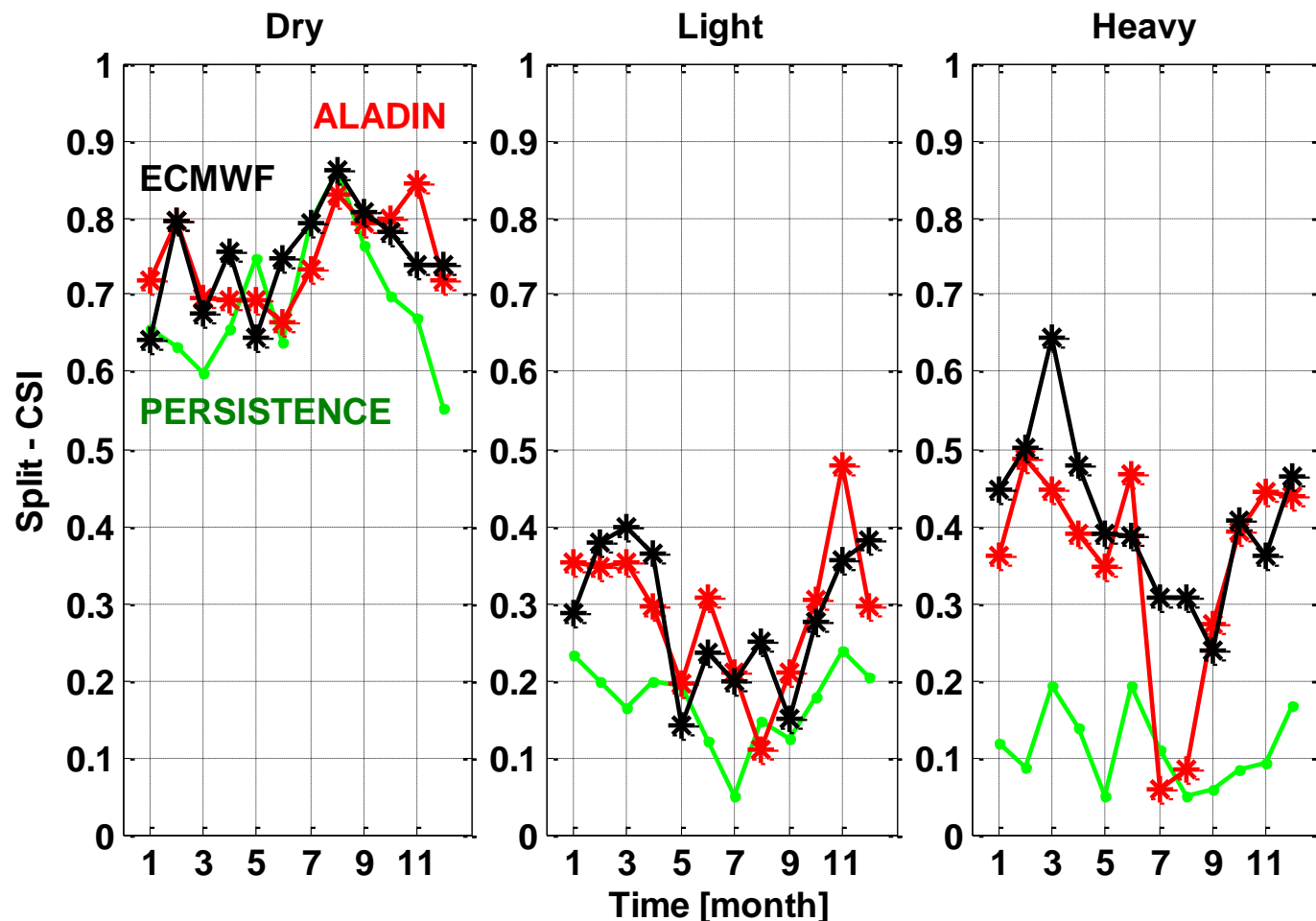
- ‘Dry’ – most probable
- Drier – less associated
- Under-forecasting ‘Dry’; over-forecasting ‘Light’ & ‘Heavy’



VERIFICATION: SPLIT

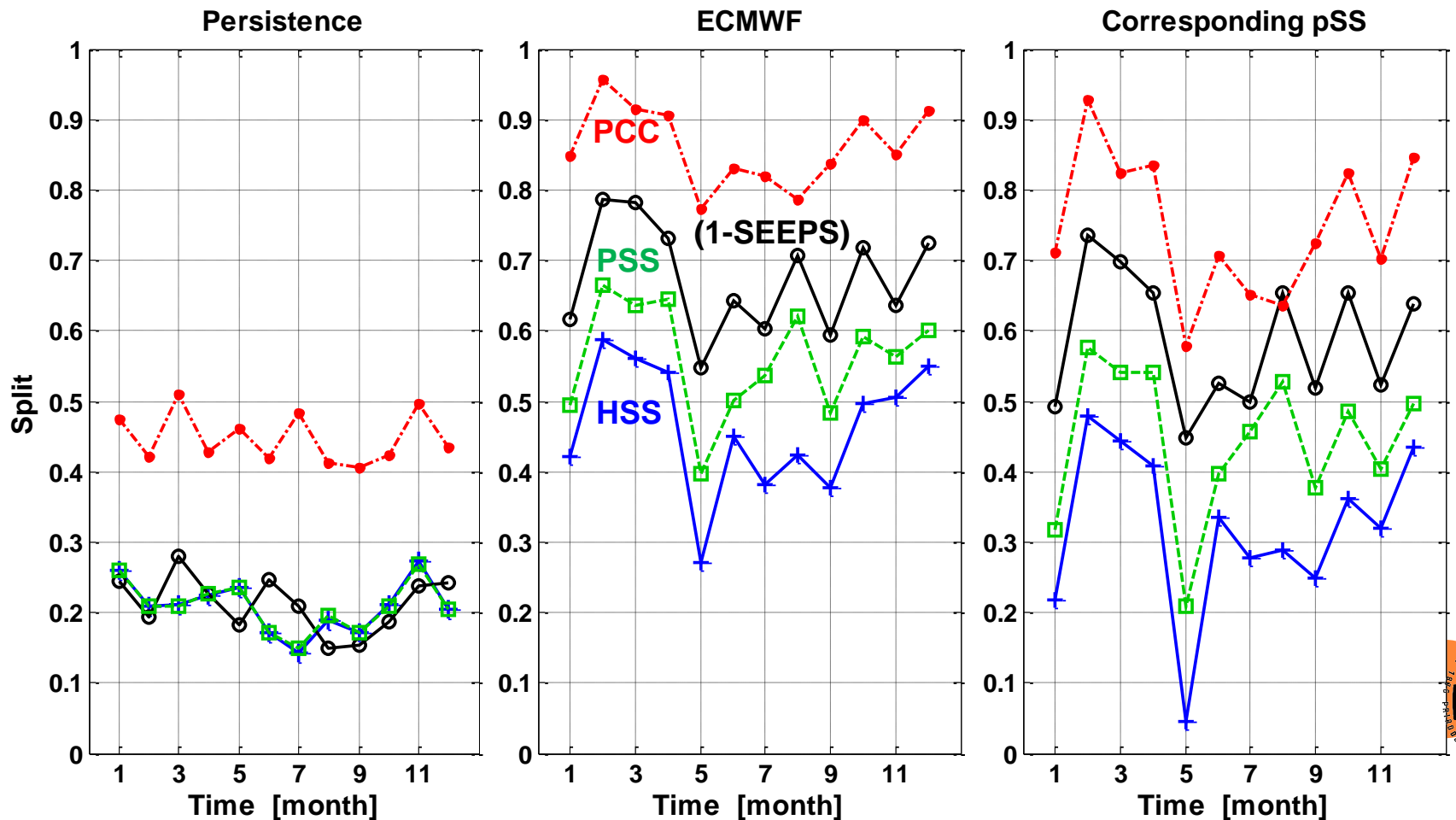
○ CSI:

- Highest for dominant category
- Lowest for „Light precipitation” category



SKILL SCORES - PERSISTENCY AS A REFERENCE

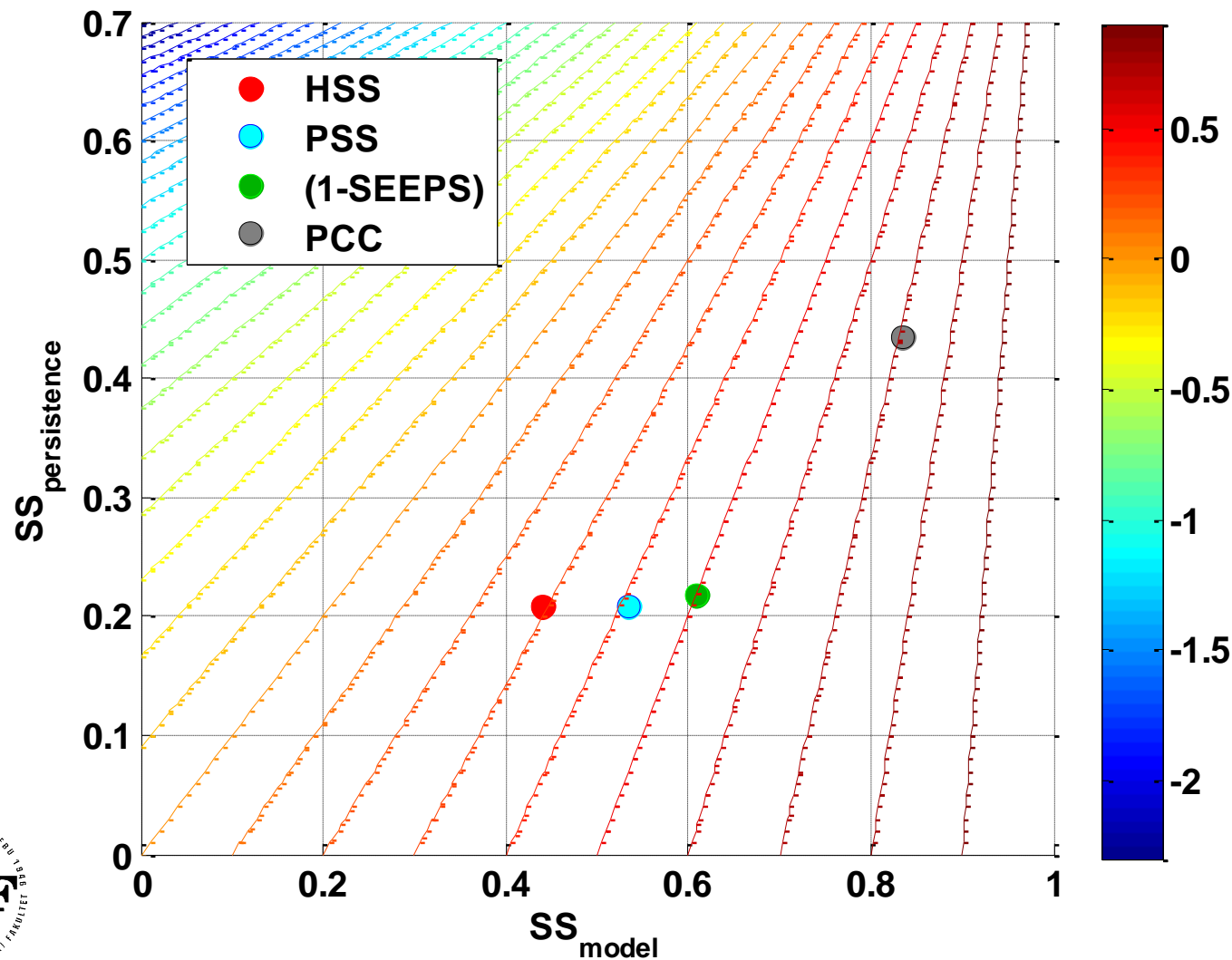
- SS generally differ in size \rightarrow pSS as well
- Shape remains similar



PERSISTENCY AS A REFERENCE:

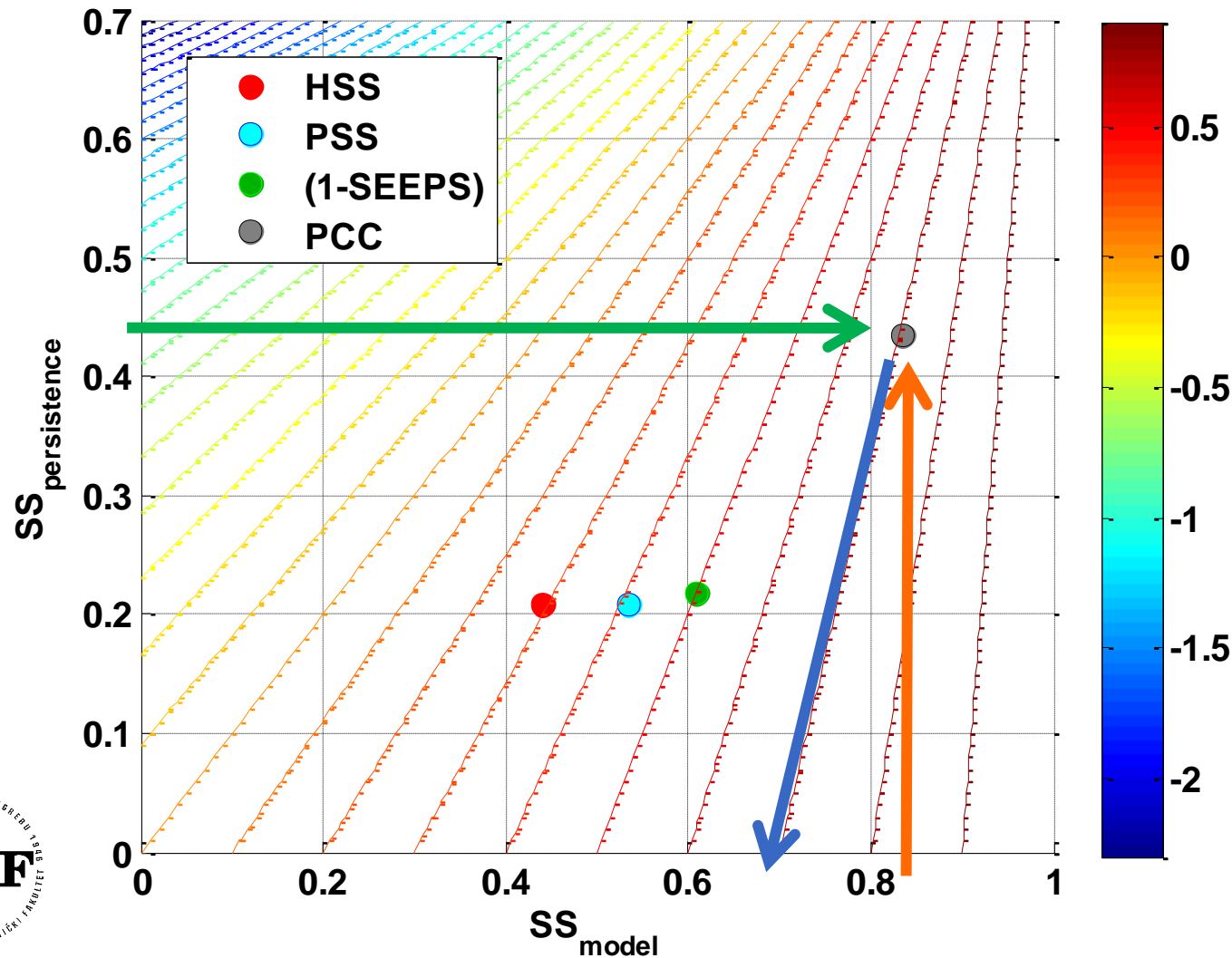
- Nomogram: contour lines for pSS

$$pSS = \frac{SS_{model} - SS_{pers.}}{SS_{ideal} - SS_{pers.}}$$

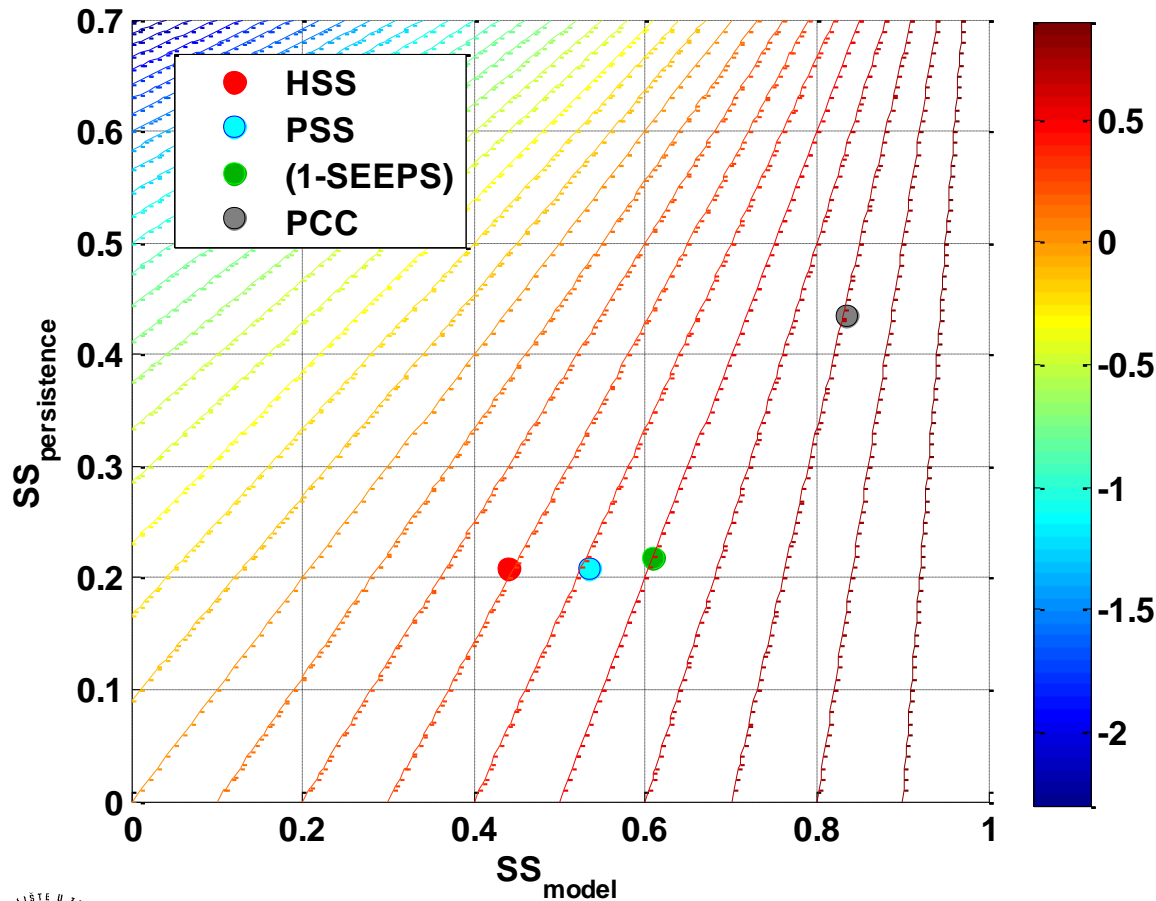


PERSISTENCY AS A REFERENCE:

$$\text{pSS} = \frac{SS_{\text{model}} - SS_{\text{pers.}}}{SS_{\text{ideal}} - SS_{\text{pers.}}}$$



PERSISTENCY AS A REFERENCE:

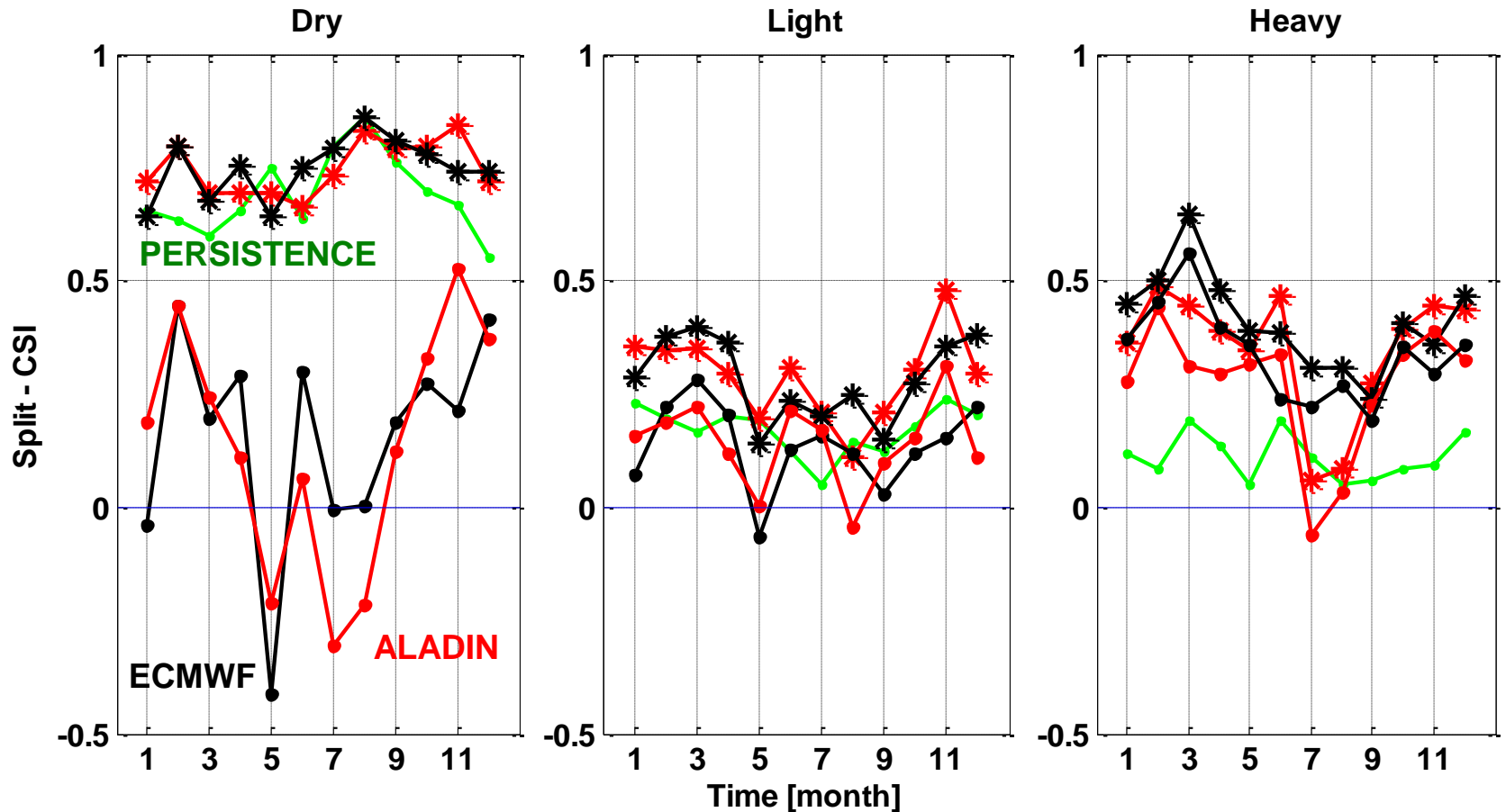


○ \overline{HSS} : low values
biggest
difference (0.14)

○ $PSS, SEEPS$: less
sensitive

○ PCC : high values
for persistency
(0.12)

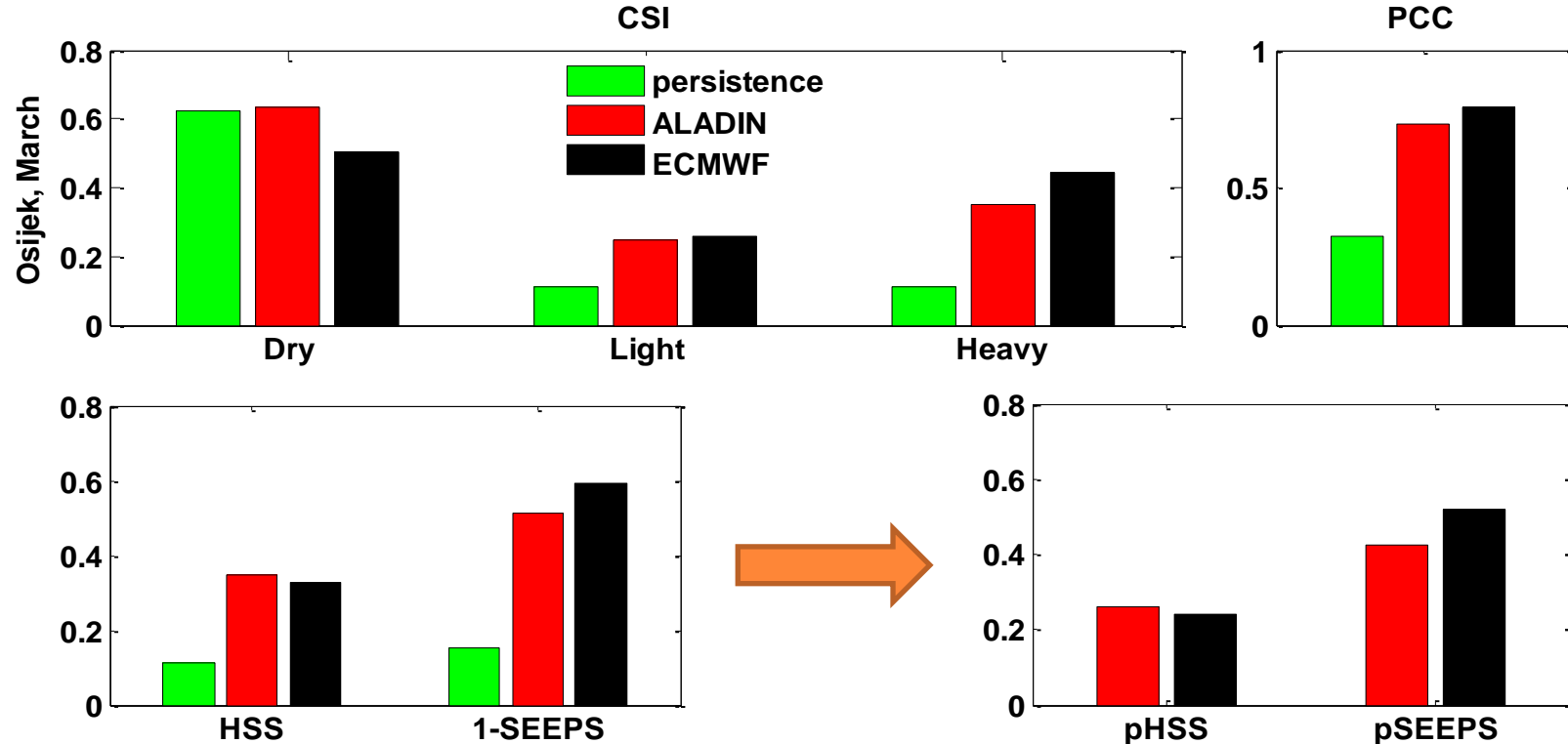
PERSISTENCY AS A REFERENCE:



- Persistence CSI_{dry} larger in May than April \rightarrow large difference
- CSI_{heavy} : in March ECMWF $>$ ALADIN \rightarrow larger difference SS and pSS
- Difference between CSI and $pCSI$:
 - largest in „Dry” category
 - Small in „Heavy” category

PERSISTENCY AS A REFERENCE:

- Inheritance of original verification measure properties



- Osijek (March):

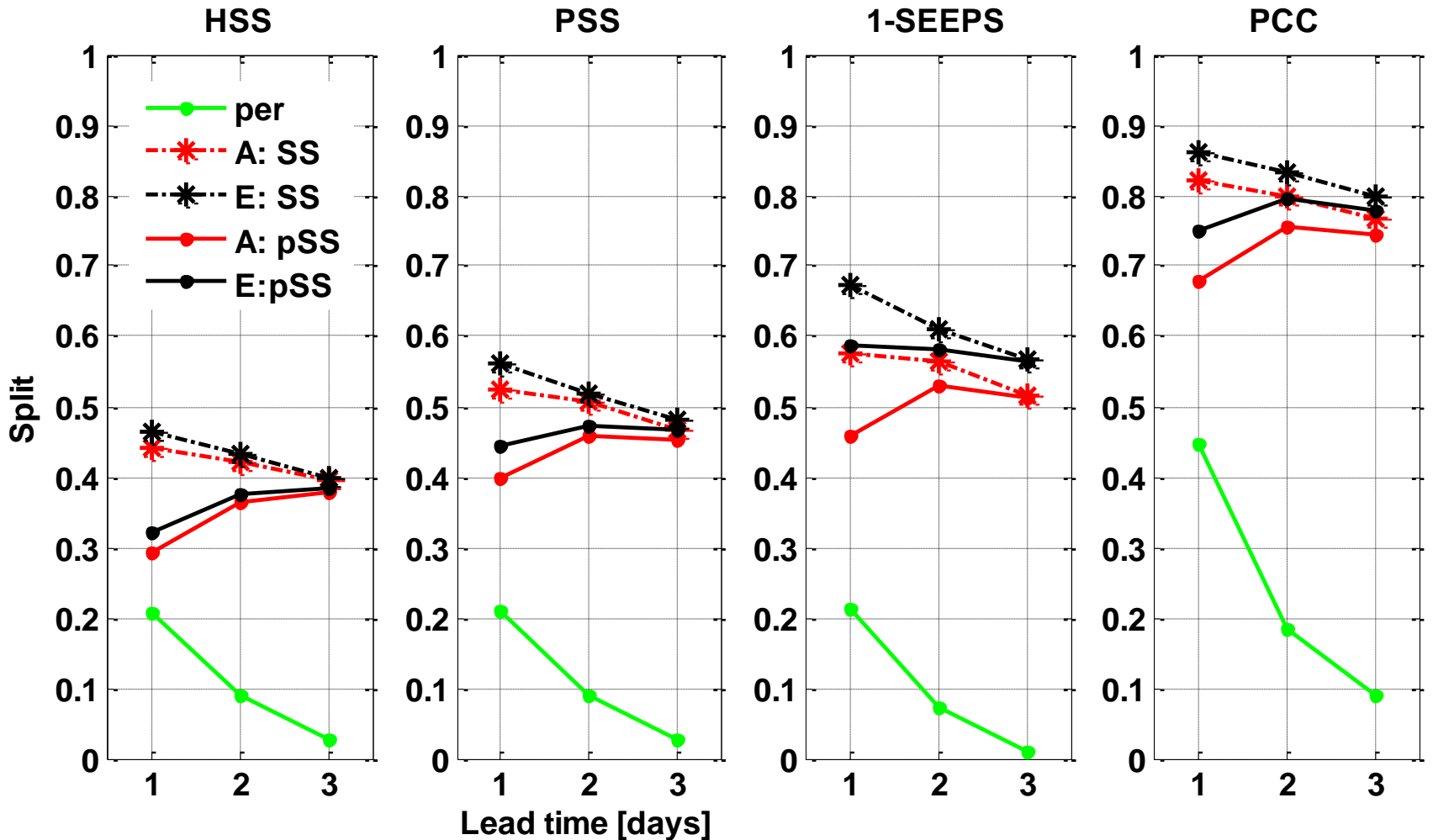
$$CSI_{dry}: ALADIN > ECMWF$$

$$CSI_{heavy}, PCC : ECMWF > ALADIN$$

→ smaller HSS for ECMWF → smaller pHSS

→ larger $(1 - SEEPS)$ → larger pSEEPS

DEPENDENCE ON LEAD TIME



- Reference: random forecast \rightarrow SS monotonically decreases
- persistency \rightarrow pSS has a maximum!!!

CONCLUSION

- pSS mostly affects the most probable category - less sensitive to climatology
- It usually maintains the similar shape as measure it is derived from and inherits properties of original measure
- Affects more measures that have smaller values in general than larger one
- Has a specific dependency on lead time that has to be taken into consideration
- Rare or extreme events → persistency as a reference makes more sense

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Questions?



THANK YOU!!!

VERIFICATION MEASURES:

- Climatological probability: $P_d = \frac{M}{P}; \quad P_l = \frac{N}{P}; \quad P_h = \frac{O}{P}$
 - Based only on observations
- Accuracy (Percent Correct): $ACC = \frac{A + F + K}{P} * 100\%$
 - Influence of P
- Frequency bias: $FBIAS_d = \frac{D}{M}; \quad FBIAS_l = \frac{H}{N}; \quad FBIAS_h = \frac{L}{O}$
 - < or > 1?

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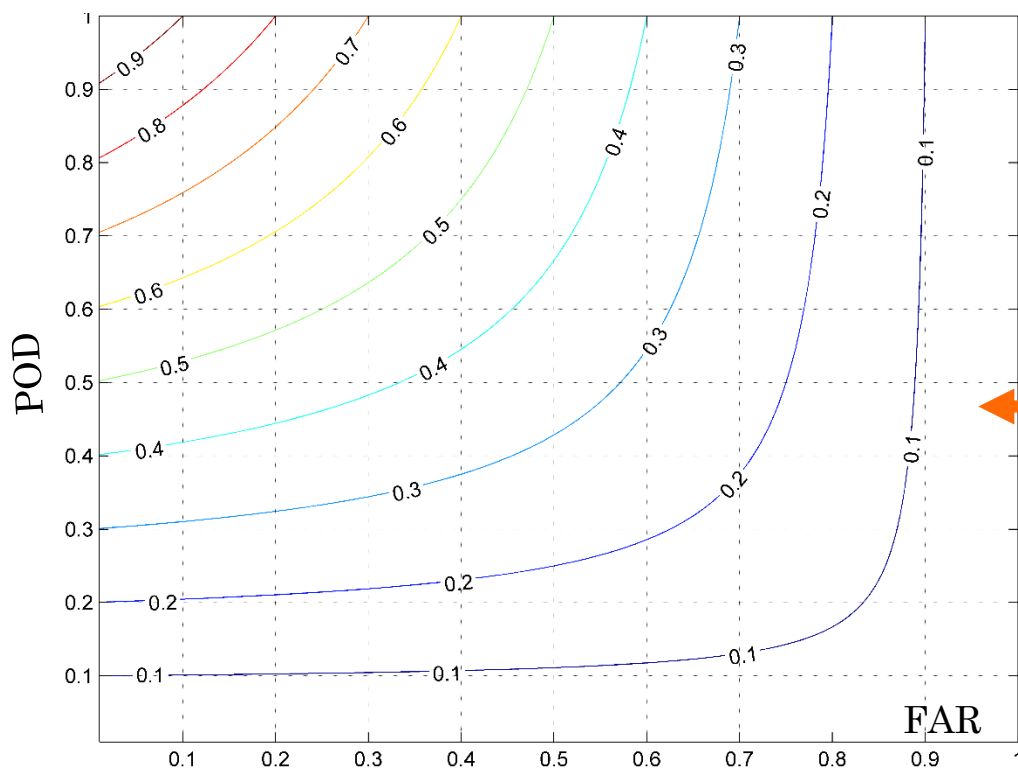


VERIFICATION MEASURES

		OBSERVATIONS			
		DRY	LIGHT	HEAVY	Σ
FORECAST	DRY	A	B	C	D
	LIGHT	E	F	G	H
	HEAVY	I	J	K	L
	Σ	M	N	O	P

○ Critical Success Index:

$$CSI_d = \frac{A}{D + M - A}; \quad CSI_l = \frac{F}{H + N - F}; \quad CSI_h = \frac{K}{O + L - K}$$



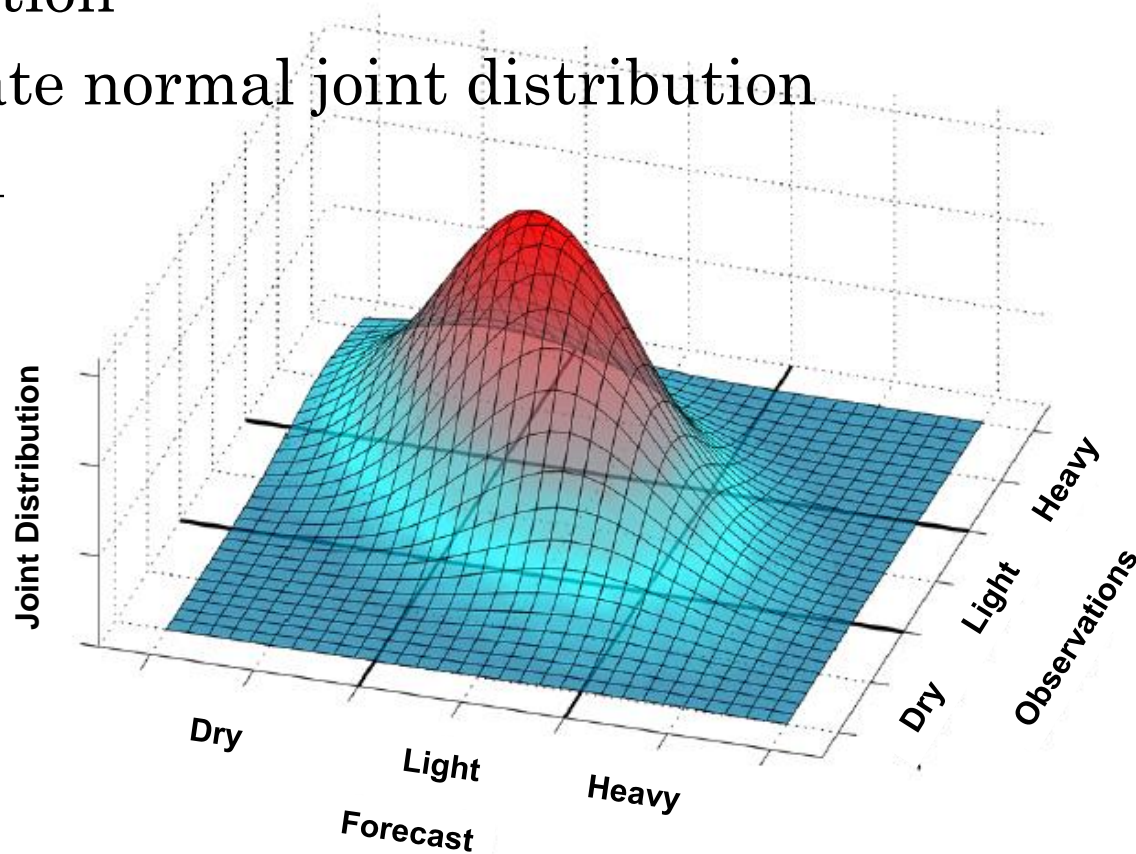
- Measure of relative accuracy:

$$CSI = \frac{1}{\frac{1}{(1 - FAR)} + \frac{1}{POD} - 1}$$



VERIFICATION MEASURES:

- Polychoric Correlation Coefficient – measure of association
- Bivariate normal joint distribution
- Ideal: 1



SKILL SCORES:

		OBSERVATIONS			
		DRY	LIGHT	HEAVY	Σ
FORECAST	DRY	A	B	C	D
	LIGHT	E	F	G	H
	HEAVY	I	J	K	L
	Σ	M	N	O	P

○ General:
$$SS = \frac{S_{prog} - S_{ref}}{S_{ideal} - S_{ref}}$$

○ Random forecast as a reference:

• Heidke Skill Score:
$$HSS = \frac{A + F + K - \frac{MD + NH + OL}{P}}{P - \frac{MD + NH + OL}{P}}$$

• Pierce Skill Score:
$$PSS = \frac{A + F + K - \frac{MD + NH + OL}{P}}{P - \frac{M^2 + N^2 + O^2}{P}}$$



SKILL SCORES:

- Persistency as a reference:

$$pCSI_k = \frac{CSI_{model,k} - CSI_{perz,k}}{1 - CSI_{perz,k}}$$

$$pPCC = \frac{PCC_{model} - PCC_{perz}}{1 - PCC_{perz}}$$

$$pHSS = \frac{HSS_{model} - HSS_{perz}}{1 - HSS_{perz}}$$

$$pPSS = \frac{PSS_{model} - PSS_{perz}}{1 - PSS_{perz}}$$

Same for (1-SEEPS), GSS and any other....

