

Development of eddy diffusivity method based on LES simulations in convective conditions

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Overview

- Review of work done/published/implemented on $K(z)$ parameterisation in stable conditions
- Extension to convective conditions: theory&application
- LES simulations turbulence resolving modelling
 - Crucial tool in developing of constructive theory of PBL sensitivity to the imposed stability
 - Kh , Km , Pr ...
 - Large-scale, semi –organized eddies driven by buoyancy forces
 - CBL-shear free, mean $V < V_{h_in}$ in large eddies
- Future work

Review: K(z) from LES stable cond.

- Methodology
 - LES data (DATABASE 64, e.g. Esau and Zilitinkevich, 2006)

Class	$w\theta_o$	N	Number	R_B	H_{LES}
Conventionally neutral	0	> 0	39	0.005 – 3.59	128 – 1652
Nocturnal	< 0	0	31	0.05 – 3.38	46 – 1875
Long-lived	< 0	> 0	15	0.35 – 7.6	16 - 507

- Each simulation was run for 15 hours to achieve a quasy steady state

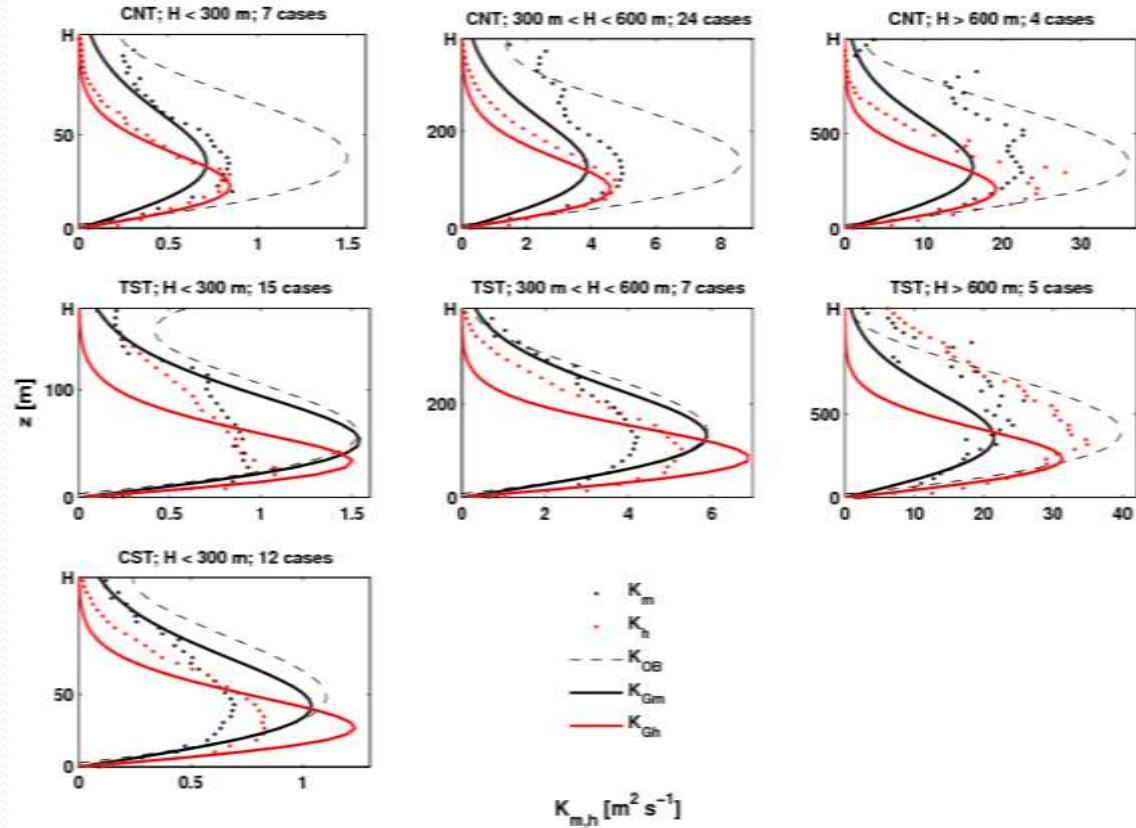
$K(z)$ –stable case (Jeričević & Večenaj 2009 BLM; Jeričević et al. 2012. ACP)

$$K_h = -\frac{\overline{w' \theta'}}{d\theta/dz} \quad (1)$$

$$K_m = k u_* z \quad (2) \text{ SL}$$

$$K_m = -\frac{\overline{u' w'}}{dU/dz} \quad (3) \text{ OL}$$

$$K(z) = (K_{\max} e^{1/2} / z_{\max}) z \exp[-0.5(z/z_{\max})^2]$$



$$\begin{aligned} K_{\max} &= C(K) H u_* \\ z_{\max} &= C(z_{\max}) H \end{aligned} \quad (4)$$

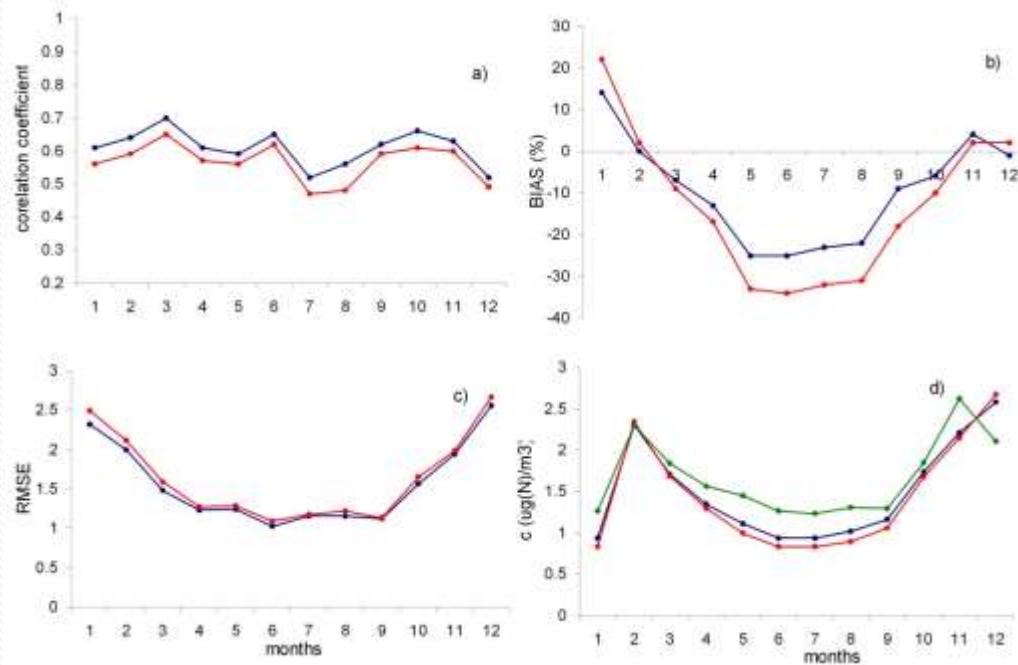
New lin-exp. function for stable conditions

	$C(K) \pm \sigma$	$C(z_{\max}) \pm \sigma$
<i>Stable</i>	$K_m (\text{m}^2 \text{s}^{-1})$	0.04 ± 0.02
	$K_h (\text{m}^2 \text{s}^{-1})$	0.05 ± 0.02

$$K(z) = C_s u_* z \exp\left(-0.5(z/0.21H)^2\right)$$

$$C_s = 0.39$$

Implemented in the operational EMEP model, (Simpson et al. 2013. ACP)



Convective LES database

- General experiment conditions
 - LESNIC v231, latitude 45N, roughness 0.1m
 - Domain size 6x6x3 km
 - Mesh 128x128x128
 - Free atmospheric stability 0.065 Km⁻¹
 - Run duration 5h-18000 s
- **A: very unstable** case characterized by low wind speed ~0.5m/s and gradually decreasing heat flux from run 1 →run 4
- **B: unstable**: run 5 and 6 have higher heat flux and wind ~1.5m/s
- **C: slightly unstable**: run 7 and 8-low heat flux wind ~1.5m/s, run 10-13 higher heat flux but with gradually increasing wind speeds
- **D: neutral**: heat flux ~0.4 and 0.25 and windy conditions > 6m/s

Wind speed	F_θ Kms ⁻¹ 0.40	F_θ Kms ⁻¹ 0.25	F_θ Kms ⁻¹ 0.07	F_θ Kms ⁻¹ 0.02
[0.5 0.0]	A run1	A run2	A run3	A run4
[1.5 0.0]	B run 5	B run 6	C run 7	C run 8
[2.5 0.0]	B run 9	C run 10		
[4.0 0.0]	C run 12	C run 13		
[6.0 0.0]	C run 14	D run 15		
[8.0 0.0]		D run 16		
[-8.0 0.]	D run 17	D run 18		

$K(z)$ profiles - convective LES

Troen & Mahrt, 1986

$$K_h = -\frac{\overline{w' \theta'}}{(d\theta/dz - \gamma_h)} \quad \gamma_h = C \frac{(\overline{w' \theta'})_0}{w_s H} \quad 5$$

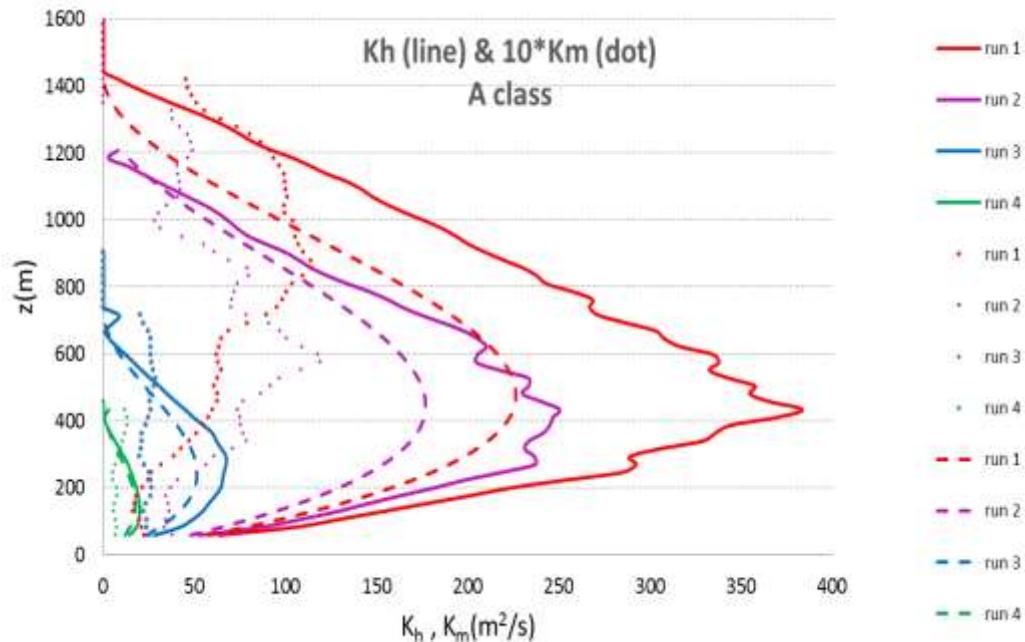
Noh et al., 2002.

$$K_m = -\frac{\overline{w' u'}}{(du/dz - \gamma_m)} \quad 6$$

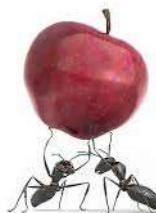
$$\gamma_m = \frac{1}{H - z_s} \int_{z_s}^H \frac{-\overline{u' w'} - K_m \partial u / \partial z}{K_m} dz$$

TM, Holtslag et al. 1990; Holtslag and Boville, 1992

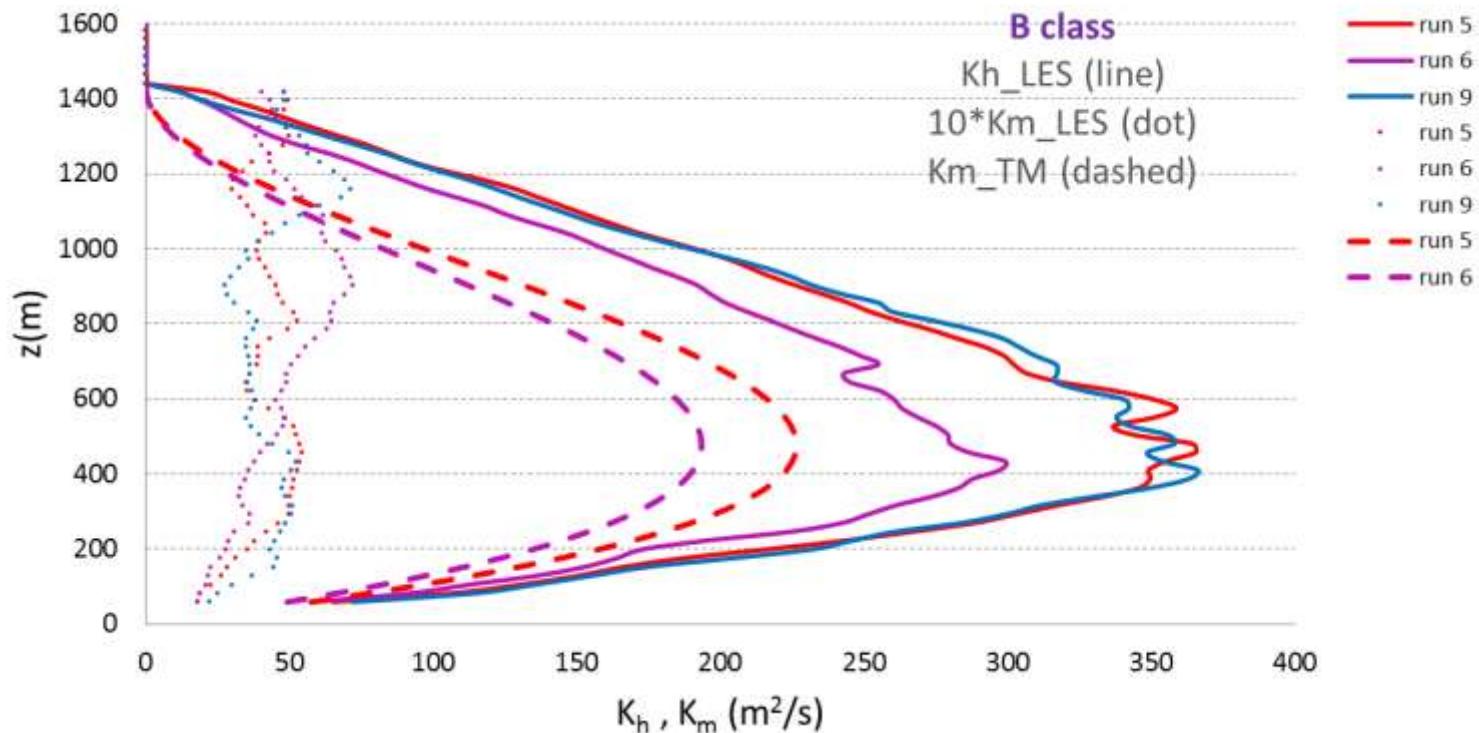
$$K_m = k w_m z \left(1 - \frac{z}{H}\right)^2 \quad 7$$



Class B

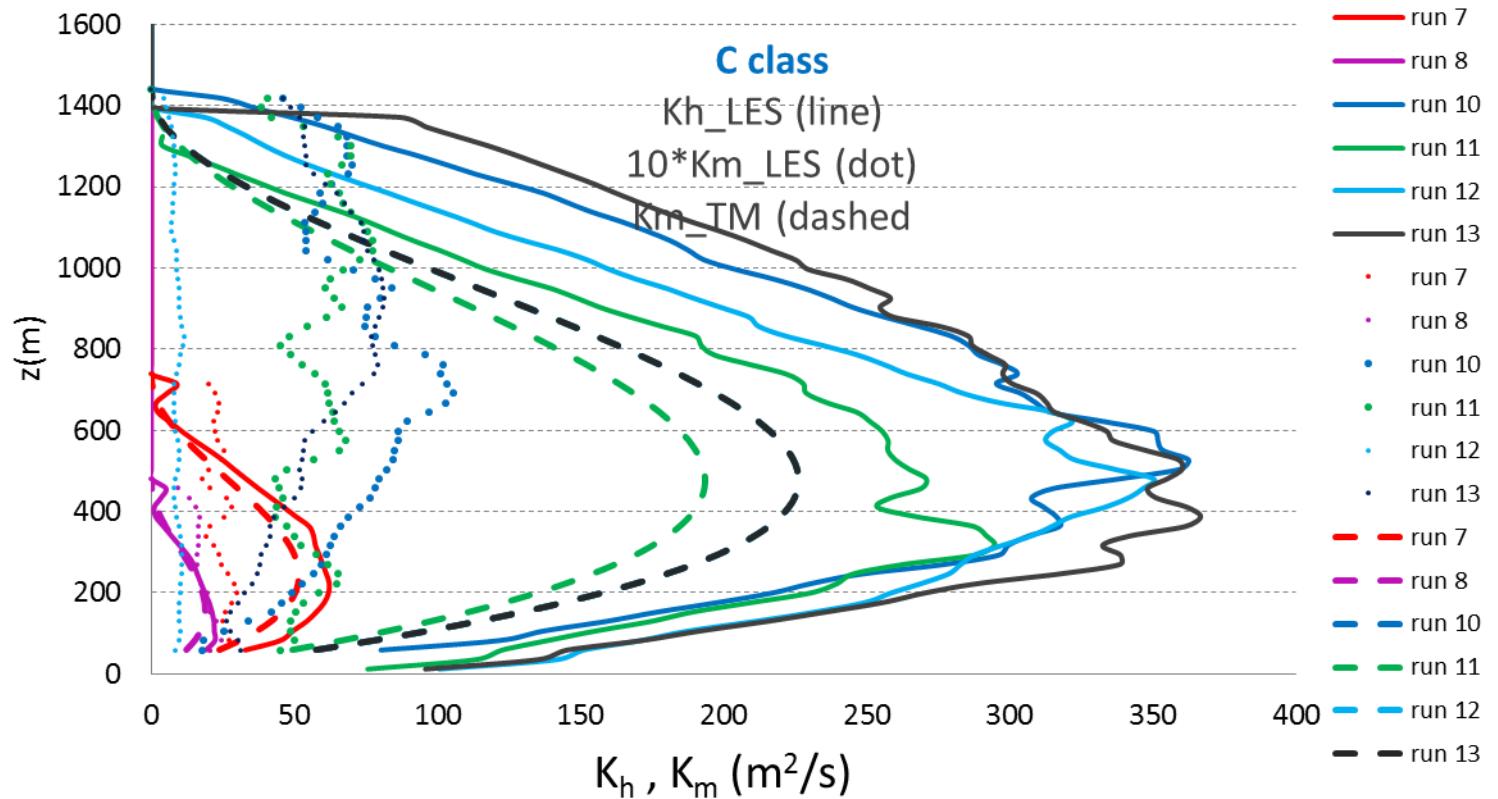


Wind speed	$F_\theta \text{ Kms}^{-1}$	$F_\theta \text{ Kms}^{-1}$	$F_\theta \text{ Kms}^{-1}$	$F_\theta \text{ Kms}^{-1}$
[0.5 0.0]	0.40	0.25	0.07	0.02
[1.5 0.0]	A run1	A run2	A run3	A run4
[2.5 0.0]	B run 5	B run 6	C run 7	C run 8
[4.0 0.0]	C run 12	C run 13		
[6.0 0.0]	C run 14	D run 15		
[8.0 0.0]		D run 16		
[-8.0 0.]	D run 17	D run 18		



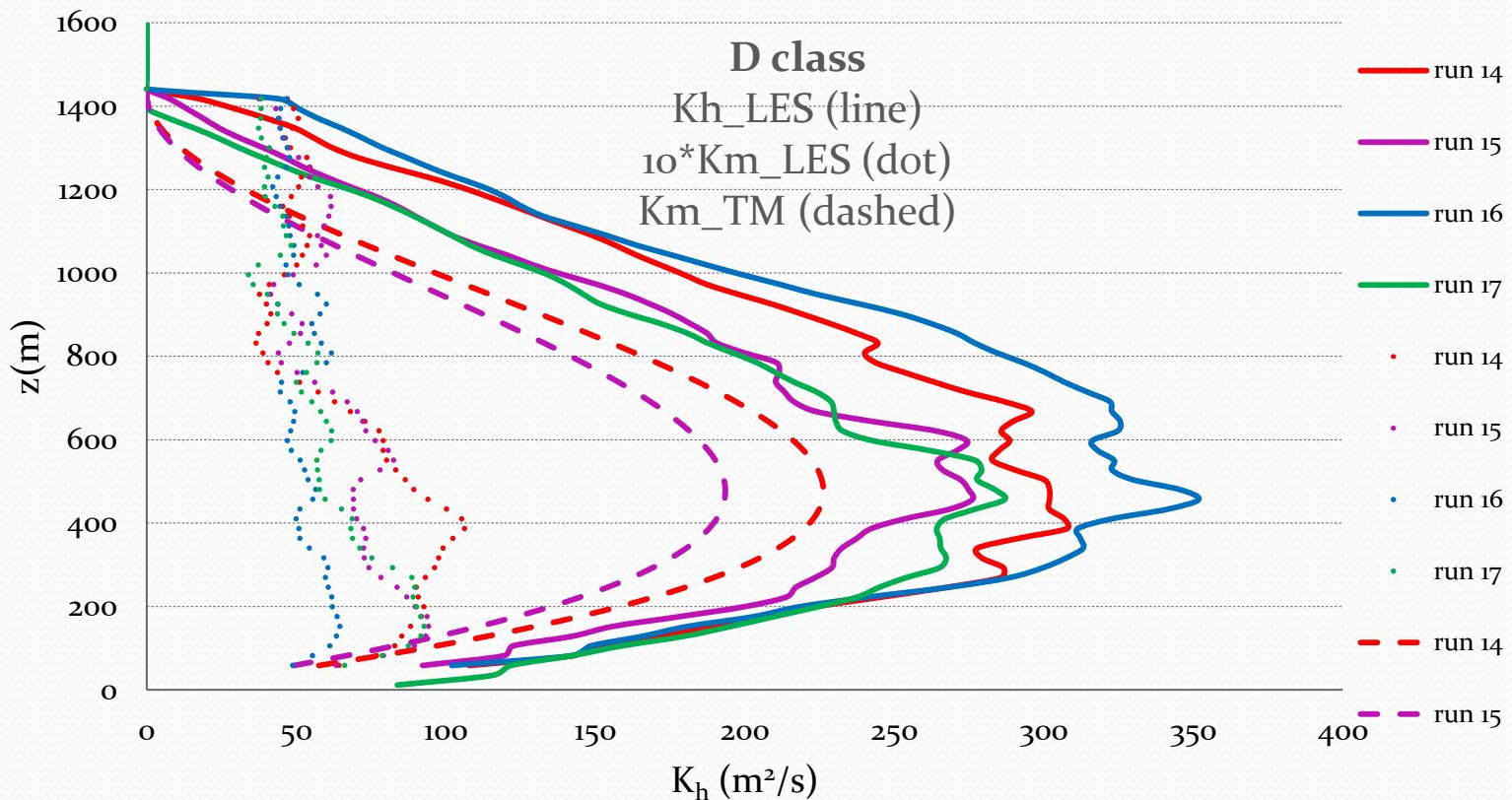
Class C

Wind speed	$F_\theta \text{ Kms}^{-1}$	$F_\theta \text{ Kms}^{-1}$	$F_\theta \text{ Kms}^{-1}$	$F_\theta \text{ Kms}^{-1}$
[0.5 0.0]	0.40	0.25	0.07	0.02
[1.5 0.0]	A run1	A run2	A run3	A run4
[2.5 0.0]	B run 5	B run 6	C run 7	C run 8
[4.0 0.0]	C run 12	C run 13		
[6.0 0.0]	C run 14	D run 15		
[8.0 0.0]		D run 16		
[-8.0 0.]	D run 17	D run 18		



D class

Wind speed	$F_\theta \text{ Kms}^{-1}$	$F_\theta \text{ Kms}^{-1}$	$F_\theta \text{ Kms}^{-1}$	$F_\theta \text{ Kms}^{-1}$
[0.5 0.0]	A run1	A run2	A run3	A run4
[1.5 0.0]	B run 5	B run 6	C run 7	C run 8
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[8.0 0.0]		D run 16		
[-8.0 0.]	D run 17	D run 18		



New K(z) formulation

$$K(z) = (K_{\max} e^{1/2} / z_{\max}) z \exp[-0.5(z/z_{\max})^2]$$

$$z_{\max} = C(z_{\max})H$$

$$K_{\max} = C(K)Hw_* \quad w_* = \left(\left(g/\theta_{v0} \right) \left(\frac{w}{\theta_v} \right)_0 H \right)^{1/3} \text{ Convective velocity scale}$$

$$K(z) = C_s u_* z \exp(-0.5(z/0.21H)^2) \quad \text{stable conditions,} \quad \mathbf{Cs=0.39}$$

$$K(z) = C_u w_* z \exp(-0.5(z/0.31H)^2) \quad \text{unstable conditions,} \quad \mathbf{Cu=1.65 \sim e^{1/2}}$$

Conclusions

- K_m does not vary significantly with stability $< 10m^2/s$
- In stable conditions
 - K_m described by exp. or polynomial,
 - similar to K_h
 - $Pr \gg 1$ with increasing stability
- In convective conditions,
 - with height but not significantly in almost constant & small range with height and with $Pr = K_m/K_h \ll 1$ since $K_h \gg K_m$
- Applied K_m based on TM, Holtslag significantly overestimates K_m
 - $Pr/Pr_{TM} = 0,131579$ i.e. Pr is overestimated $\sim 7,6$ times by TM approach!
- Theory: Are some mechanism(s) missing? Are the parameterisations wrong?

Conclusions-cont.

- Future work
 - implementation and verification
 - WRF, EMEP
 - Inclusion of entrainment layer in parametrisations